Write your name here


## Mathematics A <br> Paper 4H

Higher Tier
Tuesday 20 May 2014 - Afternoon
Time: 2 hours
Paper Reference
4MAO/4H
KMA0/4H

## You must have:

Total Marks
Ruler graduated in centimetres and millimetres, protractor, compasses, pen, HB pencil, eraser, calculator. Tracing paper may be used.

## Instructions

- Use black ink or ball-point pen.
- Fill in the boxes at the top of this page with your name, centre number and candidate number.
- Answer all questions.
- Without sufficient working, correct answers may be awarded no marks.
- Answer the questions in the spaces provided
- there may be more space than you need.
- Calculators may be used.
- You must NOT write anything on the formulae page. Anything you write on the formulae page will gain NO credit.


## Information

- The total mark for this paper is 100.
- The marks for each question are shown in brackets - use this as a guide as to how much time to spend on each question.


## Advice

- Read each question carefully before you start to answer it.
- Check your answers if you have time at the end.


## International GCSE MATHEMATICS <br> FORMULAE SHEET - HIGHER TIER

Pythagoras'


Volume of cone $=\frac{1}{3} \pi r^{2} h$
Curved surface area of cone $=\pi r l$


Volume of sphere $=\frac{4}{3} \pi r^{3}$
Surface area of sphere $=4 \pi r^{2}$



$$
\begin{aligned}
& \text { adj }=\text { hyp } \times \cos \theta \\
& \text { opp }=\text { hyp } \times \sin \theta \\
& \text { opp }=\operatorname{adj} \times \tan \theta
\end{aligned}
$$

In any triangle $A B C$

$$
\text { or } \quad \sin \theta=\frac{\text { opp }}{\text { hyp }}
$$

$$
\cos \theta=\frac{\text { adj }}{\text { hyp }}
$$



$$
\tan \theta=\frac{\mathrm{opp}}{\mathrm{adj}}
$$

Sine rule: $\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}$
Cosine rule: $a^{2}=b^{2}+c^{2}-2 b c \cos A$

Area of triangle $=\frac{1}{2} a b \sin C$


Circumference of circle $=2 \pi r$
Area of circle $=\pi r^{2}$


Volume of cylinder $=\pi r^{2} h$
Curved surface area
of cylinder $=2 \pi r h$

Area of a trapezium $=\frac{1}{2}(a+b) h$


The Quadratic Equation
The solutions of $a x^{2}+b x+c=0$, where $a \neq 0$, are given by

$$
x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}
$$

## Answer ALL TWENTY FIVE questions.

## Write your answers in the spaces provided.

## You must write down all stages in your working.

1 In the 2012 Paralympic Games, the total number of gold and silver medals won by Brazil was 35
The ratio of the number of gold medals that Brazil won to the number of silver medals that Brazil won was $3: 2$

How many silver medals were won by Brazil?

2 Sarah has a biased 4-sided spinner.
The spinner can land on 1,2, 3 or 4
The probability that the spinner will land on 1,2 or 4 is given in the table.

| Number | 1 | 2 | 3 | 4 |
| :--- | :---: | :---: | :---: | :---: |
| Probability | 0.4 | 0.35 |  | 0.1 |

(a) Work out the probability that the spinner will land on 3

Ryan is going to spin the spinner 80 times.
(b) Work out an estimate for the number of times he should expect the spinner to land on 2


Diagram NOT
accurately drawn
(a) A circle has a radius of 7.6 cm .

Work out the area of the circle.
Give your answer correct to 3 significant figures.

The radius, 7.6 cm , is correct to 1 decimal place.
(b) (i) Write down the upper bound of the radius.
cm
(ii) Write down the lower bound of the radius.
$\qquad$

Do NOT write in this space.

4 In a sale, all normal prices are reduced by $15 \%$.
(a) The normal price of a washing machine is 270 dollars.

Work out the sale price of the washing machine.
dollars
(b) The normal price of a food processor is reduced by 13.50 dollars.

Work out the normal price of the food processor.
dollars

5 Work out the size of each exterior angle of a regular polygon with 15 sides.

## Do NOT write in this space.

6 Jalin lives in England.
He does a search on the internet and sees the same type of camera on sale in France and in America.

In France, the camera costs 126 euros.
In America, the camera costs $\$ 165.24$
Jalin finds out these exchange rates.

## Exchange rates <br> 1 euro $=£ 0.89$ $£ 1=\$ 1.62$

How much cheaper is the camera in America than in France?
Give your answer in pounds (£).

7 Use ruler and compasses to construct the bisector of angle $A B C$. You must show all your construction lines.

(Total for Question 7 is 2 marks)

8


Diagram NOT accurately drawn

Calculate the length of $A C$.
Give your answer correct to 3 significant figures.

9 (a) Solve $7 x-6=2 x+17$
Show clear algebraic working.

$$
x=.
$$

(b) Expand and simplify fully $(x+8)(x+2)$

10 The table shows information about the times, in minutes, taken by 50 people to get to work.

| Time taken ( $\boldsymbol{t}$ minutes) | Frequency |
| :---: | :---: |
| $0<t \leqslant 10$ | 6 |
| $10<t \leqslant 20$ | 10 |
| $20<t \leqslant 30$ | 19 |
| $30<t \leqslant 40$ | 15 |

Work out an estimate for the mean time taken to get to work.

11 (a) Complete the table of values for $y=x^{2}+2 x-3$

| $x$ | -4 | -3 | -2 | -1 | 0 | 1 | 2 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ |  | 0 | -3 | -4 |  |  | 5 |

(b) On the grid, draw the graph of $y=x^{2}+2 x-3$ for values of $x$ from -4 to 2

(2)

12 The diagram shows triangle $A D C$.


Diagram NOT
accurately drawn
$E$ is a point on $A D$ and $B$ is a point on $A C$ so that $E B$ is parallel to $D C$.
$A B=14 \mathrm{~cm}$.
$E B=16 \mathrm{~cm}$.
$D C=20 \mathrm{~cm}$.
Calculate the length of $B C$.
cm

Do not write in this space.

13 The line $\mathbf{L}$ passes through the points $(0,-2)$ and $(6,1)$
(a) Find an equation of the line $\mathbf{L}$.
(b) Find an equation of the line that is parallel to $\mathbf{L}$ and which passes through the point $(4,-2)$

14 (a) Write $1.2 \times 10^{-5}$ as an ordinary number.
(b) Work out $7.9 \times 10^{5}+6 \times 10^{4}$

Give your answer in standard form.

15 Solve the simultaneous equations

$$
\begin{aligned}
& 3 x+2 y=7 \\
& 4 x-3 y=15
\end{aligned}
$$

Show clear algebraic working.
$x=$
$y=$

(a) $P, Q$ and $R$ are points on a circle, centre $O$.

Angle $O P R=36^{\circ}$
Work out the size of angle $P Q R$.
Diagram NOT
accurately drawn

Diagram NOT accurately drawn
(b) $G, H, J$ and $K$ are points on a circle.
$K J$ is a diameter of the circle.
Angle $K G H=124^{\circ}$
Work out the size of angle $H K J$.
$17 F$ is inversely proportional to the square of $x$.
$F=0.8$ when $x=5$
(a) Find a formula for $F$ in terms of $x$.
(b) Work out the positive value of $x$ when $F=320$

Do NOT write in this space.

18 (a) Solve $5 x^{2}-6 x-2=0$
Give your solutions correct to 3 significant figures.
Show your working clearly.
(b) Solve the inequality $\frac{m^{2}+3}{4}>21$

Show clear algebraic working.

19 Amberish plays two games of tennis.
Each time he plays a game of tennis, the probability that he will win is $\frac{2}{7}$
(a) Complete the probability tree diagram.

First game
Second game

(b) Calculate the probability that Amberish wins at least one of the two games of tennis.

20 Use algebra to show that the recurring decimal $0.3 \dot{8}=\frac{7}{18}$

21 A sphere has a surface area of $81 \pi \mathrm{~cm}^{2}$.
Work out the volume of the sphere.
Give your answer correct to 3 significant figures.

$\mathrm{cm}^{3}$

22 The table shows information about the times, in minutes, that 100 shoppers spent in a supermarket.

| Time $(\boldsymbol{t}$ minutes) | Frequency |
| :---: | :---: |
| $10 \leqslant t<15$ | 6 |
| $15 \leqslant t<20$ | 10 |
| $20 \leqslant t<30$ | 20 |
| $30 \leqslant t<40$ | 36 |
| $40 \leqslant t<60$ | 28 |

Draw a histogram to show this information.


Do NOT write in this space.

23

$A B C D E F$ is a triangular prism.
$A B=9 \mathrm{~cm}, B C=15 \mathrm{~cm}$ and $A E=12 \mathrm{~cm}$.
Angle $A B C=90^{\circ}$
$M$ is the midpoint of $C D$.
Calculate the size of the angle between $A M$ and the plane $B C D F$.
Give your answer correct to 1 decimal place.

24 Given that $\quad\left(2^{\frac{1}{2}}\right)^{n}=\frac{2^{x}}{8^{y}}$
express $n$ in terms of $x$ and $y$.

25 Simplify fully $\frac{5}{2 x-6}-\frac{x+2}{x^{2}-4 x+3}$

